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Acknowledgements



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• Introduction

YBCO: spin and charge
BSCCO: got nematic?

• Look out









Crystal

Т



Crystal

Т

Liquid

Nematic











Sufficiently correlated systems





License to exist?

Quantifying broken symmetry

License to exist?

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> Phenomenological model

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Why would cuprates do that?

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Is it useful for superconductivity?

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Nematic QCP, license to exist?

PHYSICAL REVIEW B 77, 184514 (2008)

Theory of the nodal nematic quantum phase transition in superconductors

Eun-Ah Kim,¹ Michael J. Lawler,² Paul Oreto,¹ Subir Sachdev,³ Eduardo Fradkin,³ and Steven A. Kivelson¹ ¹Department of Physics, Stanford University, Stanford, California 94305, USA ²Department of Physics, University of Toronto, Toronto, Ontario, Canada ³Department of Physics, University of Illinois at Urbana-Champaign, 1110 West Green Street, Urbana, Illinois 61801-3080, USA (Received 15 February 2008; published 22 May 2008)

• Nodal nematic QCP deep inside d-wave SC

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nematic QCP inside SC phase?

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• Nodal nematic QCP deep inside d-wave SC

• Nematic d-SC: d-SC + small s-component $\Delta_d (\cos k_x - \cos k_y) + \lambda \phi$



nematic QCP inside SC phase?

Looking for nematic critical fluctuations

•Self energy $\hat{\Sigma}(\vec{q}, \omega)$ due to fluctuation :k-selective decoherence



Interference of nematic quantum critical quasiparticles: a route to the octet model

Eun-Ah Kim^1 and Michael J. Lawler^{2, 1}

¹Department of Physics, Cornell University, Ithaca, NY 14853 ²Department of Physics, Binghamton University, Binghamton NY 13902 (Dated: November 13, 2008)

arXiv:0811.2242



YBCO, spin and charge





Anisotropy in inelastic $(\pi/a,\pi/b)$ neutron scattering peak Hinkov et al, Science, Jan 2008

Spin channel





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Spin channel

Incommensurability as Order parameter?

 $\delta \propto \sqrt{T - T^*}$





Spin channel

Charge channel

Kai Sun,^{1,2} Michael J. Lawler,^{3,4} and Eun-Ah Kim⁴

arXiv:0906.3460

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$$S[\vec{\phi}] = \frac{1}{g} \int \frac{d^2 \mathbf{q} d\omega}{(2\pi)^3} \left(i\Gamma |\omega| + \omega^2 - \Delta^2 \left(\mathbf{q}\right) \right) |\vec{\phi}(\mathbf{q},\omega)|^2.$$



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$$\Delta^2(\mathbf{q};N) = \Delta_0^2(N) + c_0^2(N)q^2 - c_2^2(N)N(q_x^2 - q_y^2) + \cdot$$

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Spin-charge interplay in electronic liquid crystals: fluctuating spin stripe driven by charge nematic

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BSCCO, got nematic?



 $\begin{array}{c} dI/dV(\omega)\text{-map}\\ \text{McElroy et al, Nature 422, 592 (2003)}\\ \text{OD }T_c\text{=}86\text{K}\ (\text{p=}\) \end{array}$





0.69

Figure S7 a-f. A series of images displaying the real space conductance ratio *Z* as a function of energy rescaled to the local psuedogap value, $e = E/\Delta_1(\mathbf{r})$. Each pixel location was rescaled independently of the others. The common color scale illustrates that the bond centered pattern appears strongest in *Z* exactly at $E = \Delta_1(\mathbf{r})$.

Z-map(ω) Kohsaka et al, Nature 454, 1072 (2008) UD T_c=45K

R-map Kohsaka et al, Science 315, 1380 (2007) UD T_c=45K (p=0.08)

HAMLET: Do you see yonder cloud that's almost in shape of a camel?

POLONIUS: By th'mass, and 'tis like a camel indeed.

HAMLET: Methinks it is like a weasel.

POLONIUS: It is backed like a weasel.

--W. Shakespeare (S. Chakravarty's perspectives Science 08)



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M. Lawler et al, in prep. Challenge: An objective measure

Candidate broken symmetries

2.7

2.4

2.1

1.8

1.5

1.2

0.9

0.6

Z-map intensity at E = 150.0meV



Translational symmetry \hat{T}_a, \hat{T}_b Rotational symmetry $\hat{R}_{\pi/2}$

Can we separately measure?

Need a \hat{T}_a, \hat{T}_b preserving order parameter

On the shoulder of

• Relating asymmetry to a quantitative measure $Z(\mathbf{r}, \mathbf{w}) = R(\mathbf{r})$

P. Anderson, N.P. Ong J. Phys. Chem. Solids, **67**,1(1993) M.B.J. Meinders, H. Eskes, G.A. Sawatzky Phys. Rev. B, **48**, 3916 (1993)

M. Randeria et al, PRL **95**, 137001 (2005)

• Fourier filtering to look for stripe

$$N_f(\mathbf{r}, E) = \int d\mathbf{r}' f(\mathbf{r} - \mathbf{r}') N(\mathbf{r}', E), \qquad f(\mathbf{r}) \propto \Lambda^2 e^{-r^2 \Lambda^2/2} [\cos(\pi x/2a) + \cos(\pi y/2a)].$$

C. Howald et al, S. Kivelson et al, PRB **67**, 014533 (2003) RMP **75**, 1201 (2003)

Z-map intensity at E = 150.0meV



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Q_x vs Q_y? S_x vs S_y

Listen to Bragg Peaks



• Bragg peak $\tilde{Z}(\vec{Q}_x) = \frac{1}{\sqrt{N}} \sum_{\vec{R}+\vec{d}} Z(\vec{R}+\vec{d})e^{-i\vec{Q}_x \cdot \vec{d}}$ $\vec{Q}_x = (2\pi/a, 0)$

• Need O sites $\tilde{Z}(\vec{Q}_x) = \bar{Z}_{Cu} - \bar{Z}_{O_x} + \bar{Z}_{O_y}, \quad \tilde{Z}(\vec{Q}_y) = \bar{Z}_{Cu} + \bar{Z}_{O_x} - \bar{Z}_{O_y}$ $\mathcal{O}_N \propto (\bar{Z}_{O_x} - \bar{Z}_{O_y})$





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Nematic ordering in UD 45



Extracted from published data, T=4K

Kohsaka et al, Nature 454, 1072 (2008)

Qy

 Q_X

 \odot

Domain size in Z-map

Domain size in Z-map



Nematic domains

• Shift Q_x, Q_y to origin ("tune to the channel")



• Low pass filter (long distance physics)



Nematic domains

• Shift Q_x, Q_y to origin ("tune to the channel")

• Low pass filter (long distance physics)

0.008

0.006

0.004

0.002

0.000

-0.002

-0.004

-0.006

-0.008



Listen to channel S

Oriented stripe domains

• Shift S_x, S_y to origin ("tune to the channel")

 Q_{X}

→ •] dia

• Low pass filter (long distance physics)



Qy

VOLUME 66, NUMBER 24

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17 JUNE 1991

Weak Pinning and Hexatic Order in a Doped Two-Dimensional Charge-Density-Wave System

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